

1. What is the end behavior of the polynomial function $f(x) = -2x^5 + 3x^3 - x + 4$?
- a) $f(x)$ approaches infinity as x approaches infinity, and $f(x)$ approaches infinity as x approaches negative infinity.
 - b) $f(x)$ approaches negative infinity as x approaches infinity, and $f(x)$ approaches negative infinity as x approaches negative infinity.
 - c) $f(x)$ approaches negative infinity as x approaches infinity, and $f(x)$ approaches infinity as x approaches negative infinity.
 - d) $f(x)$ approaches infinity as x approaches infinity, and $f(x)$ approaches negative infinity as x approaches negative infinity.
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2. Identify the vertical asymptote(s) of the rational function $f(x) = \frac{(2x^2 + 3x)}{(x^2 - 4)}$:
- a) $x = -2$ and $x = 2$
 - b) $x = 0$
 - c) $x = -4$ and $x = 4$
 - d) No vertical asymptotes
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3. What is the degree and leading coefficient of the polynomial function $f(x) = 4x^3 - 7x^2 + 5x - 2$?
- a) Degree 3, leading coefficient 4
 - b) Degree 4, leading coefficient 4
 - c) Degree 3, leading coefficient -7
 - d) Degree 4, leading coefficient -7
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4. Which of the following is the simplified form of $\frac{(x^2 - 4)}{(x^2 - x - 6)}$?
- a) $(x - 2) / (x - 3)$
 - b) $(x + 2) / (x - 3)$
 - c) $(x - 2) / (x + 3)$
 - d) $(x + 2) / (x + 3)$
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5. Factor the polynomial $f(x) = x^4 - 5x^2 + 4$ completely.

6. Sketch the graph of $f(x) = \left(\frac{2}{x-3}\right) + 1$. Indicate the vertical asymptote, horizontal asymptote, and any intercepts.

7. Find the equation of a polynomial function with roots $x = 1, x = -2, x = 3$ and degree 3, if its leading coefficient is 2.

8. Solve the inequality $\frac{(2x+1)}{(x-4)} \leq 0$ and represent the solution on a number line.

9. A company's profit can be modeled by the polynomial $P(x) = -2x^3 + 12x^2 - 20x + 5$, where x represents the number of items produced in thousands.

- a) Find the profit when $x = 3$.
 - b) Determine the number of items produced that maximizes profit by finding the critical points of $P(x)$.
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10. For the rational function $f(x) = \frac{(x^2 - 2x - 3)}{(x^2 - 9)}$:

- a) Determine the vertical and horizontal asymptotes.
 - b) Identify any removable discontinuities.
 - c) Sketch the graph, clearly labeling key features.
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11. Given the polynomial $f(x) = x^3 - 4x^2 + x + 6$:

- a) Use synthetic division to determine if $x - 2$ is a factor of $f(x)$.
 - b) Fully factor $f(x)$.
 - c) Sketch the graph, labeling all intercepts and describing the end behavior.
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12. Real-World Application Problem:

A rectangular storage container with an open top has a volume of 1000 cubic meters. The width is twice the length. The cost of materials for the base is \$10 per square meter, and the cost for the sides is \$5 per square meter. Write a rational function for the cost of the materials as a function of the length of the base and determine the dimensions that minimize the cost.